

STRENGTH OF MATERIALS I
 1st Mid-Term Exam
 04/10/2013
 Solutions

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1) a)

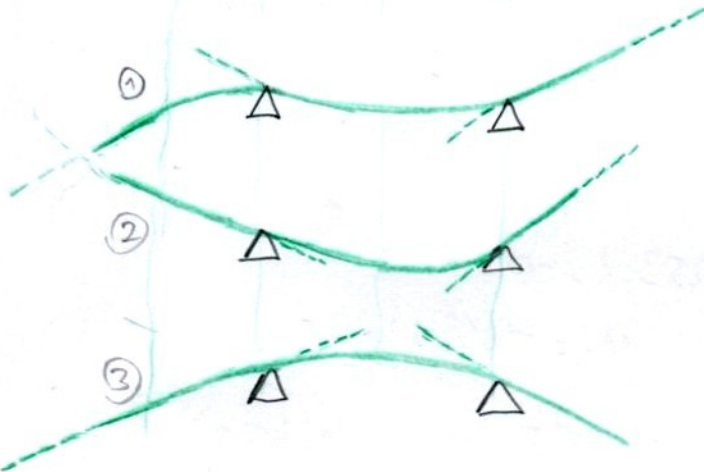
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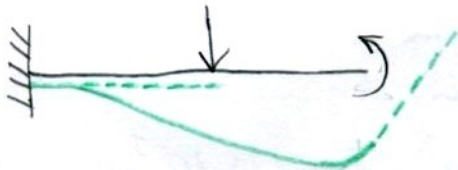
● Displaced state
 --- Tangent line at support

b)

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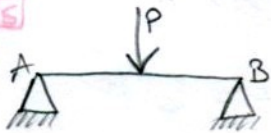


5 c)



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2) a)



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b) $w, h, \text{ material, support conditions}$

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c) You can increase the strength by

- Changing the material
- Increasing the cross-section parameters w, h

30) 3) a) $\sum M_c = 0$

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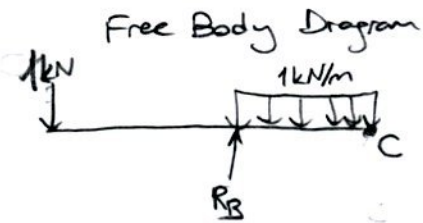
$$1 \cdot (4) + 1.2 \cdot 4 \cdot (1,2) - R_B \cdot (2,4) = 0$$

$$R_B = \underline{\underline{2,87 \text{ kN}}}$$

$$\sum \text{Load} = \sum \text{support reactions}$$

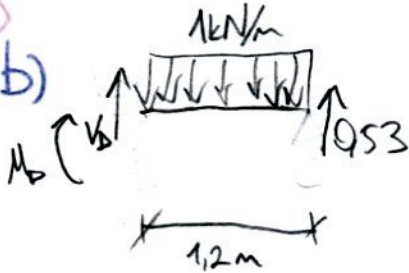
$$1 + 1.2 \cdot 4 = 2,87 + R_C$$

$$R_C = \underline{\underline{0,53 \text{ kN}}}$$



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b)



$$\sum F_y = 0$$

$$0,53 - 1 \cdot (1,2) + V_D = 0$$

$$V_D = \underline{\underline{0,67 \text{ kN}}}$$

$$\sum M_D = 0$$

$$-M_D - 1 \cdot 1,2 \cdot 0,6 + 0,53 \cdot 1,2 = 0$$

$$M_D = \underline{\underline{-0,084 \text{ kN}\cdot\text{m}}}$$

4) It is easier to work with SI units (m, kg, s)

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Specimen diameter = 10mm = 0,01m

Gage length = 50mm = 0,05m

$$\text{Area}_{\text{specimen cross section}} = \pi \cdot \left(\frac{d}{2}\right)^2 = \pi \cdot \left(\frac{0,01}{2}\right)^2 = 7,854 \cdot 10^{-5} \text{ m}^2$$

P [N]	ΔL [m]	$\sigma = P/A$ [$\frac{\text{N}}{\text{m}^2} = \text{Pa}$]	$E = \frac{\Delta L}{L_0}$ [$\frac{\text{m}}{\text{m}}$]
0	0	0	0
$8,77 \cdot 10^3$	$0,15 \cdot 10^{-3}$	$1,117 \cdot 10^8$	$3,0 \cdot 10^{-3}$
$15,3 \cdot 10^3$	$0,26 \cdot 10^{-3}$	$1,948 \cdot 10^8$	$5,2 \cdot 10^{-3}$
$182 \cdot 10^3$	$0,34 \cdot 10^{-3}$	$2,317 \cdot 10^8$	$6,8 \cdot 10^{-3}$

Apply linear regression to $E-\sigma$ data

$$y = A + Bx \quad B = 34,78 \cdot 10^9$$

\Rightarrow Therefore Modulus of Elasticity $E = \underline{\underline{34,78 \text{ GPa}}}$